

Please note that the Physics question pattern has changed for JEST 2026.  
Part A: 10 multiple choice questions each carrying 1 mark  
Part B: 20 multiple choice questions each carrying +3 marks  
Part C: 10 numericals: 3 marks  
For details, please visit the FAQ page at <https://www.jest.org.in>.

## JEST-2026 Sample Question Paper

### Part A: 1-Mark MCQ

1. A particle is moving under the force field given by  $\vec{F} = k\vec{r}$ , where  $k$  is a positive constant. The difference in work done (in arbitrary units) if the particle moves from point A  $(-1, 0, 0)$  to point B  $(1, 0, 0)$  following semi-circular paths in the clockwise and anti-clockwise directions on the X-Y plane will be
  - A. 0
  - B.  $2\pi k$
  - C.  $\frac{1}{2}\pi k$
  - D.  $\pi k$
2. The Fraunhofer diffraction pattern formed by an elliptical aperture will be
  - A. elliptical with the semi-major axis perpendicular to that of the aperture.
  - B. circular.
  - C. elliptical with the semi-major axis parallel to that of the aperture.
  - D. hyperbolic.
3. For a relativistic point particle the momentum is  $\vec{p} = \frac{m_0\vec{v}}{\sqrt{1-v^2/c^2}}$ , where  $\vec{v}$  is its velocity as measured by an inertial observer. Then the acceleration is in the same direction as the applied force
  - A. only when force is parallel or perpendicular to the velocity.
  - B. always.
  - C. never.
  - D. only when force is neither parallel nor perpendicular to the velocity.
4. For a plane electromagnetic wave propagating with wave vector  $\vec{k}$  in a homogeneous and isotropic medium, which of the following holds?
  - A.  $\vec{E} \cdot \vec{B} = 0$
  - B.  $\vec{E} \times \vec{B} = \vec{0}$
  - C.  $\vec{k} \cdot (\vec{E} \times \vec{B}) = 0$
  - D. None of the others.

5. Given the differential operator:  $D \equiv \frac{d^2}{dx^2} + P \frac{d}{dx} + Q$ , where  $P$  and  $Q$  are constants, what is the eigenvalue corresponding to the eigenfunction  $y = e^x$ ?
- $(1 + P + Q)$
  - $(P + Q)$
  - $(1 + Q)$
  - $(P + Q - 1)$
6. Suppose the mass of the Sun is reduced to half of its original value very slowly, e.g., over a billion years, what will be the effect of this on the Earth's orbit?
- Remains elliptical, but the mean radius changes.
  - Remains elliptical with the same mean radius.
  - Orbit remains closed but not elliptical.
  - The Earth flies away.
7. Consider the time-independent Schrödinger equation with a real potential and suppose  $\psi(x)$  is a solution of this equation. Which of the following is true?
- $\psi^*$  is a solution of the same equation.
  - $\psi^*$  is never a solution of the same equation.
  - $\psi^*$  is a solution of the same equation only if the potential is symmetric about  $x = 0$ .
  - $\psi^*$  is a solution of the same equation only if the potential vanishes at infinity.
8. Consider a quantum system that is evolved sequentially with a finite sequence of Hermitian Hamiltonians  $\{H_0, H_1, \dots, H_n\}$ . The full evolution operator is written as:
- $$U = U_n U_{n-1} \dots U_1 U_0 = e^{-i\mathcal{H}}, \text{ with } U_j = e^{-iH_j} \text{ and, } j = 0, 1, \dots, n$$
- Then  $U$  is
- a Hermitian operator.
  - a unitary operator.
  - undefined.
  - None of the others.

9. Consider two identical charged balls, each of mass  $m$  and charge  $q$ . One of them is initially held fixed on a frictionless insulating horizontal surface and the other is carefully placed above the first one at a height  $h$  from the surface, such that the gravitational force on it is balanced by the Coulomb repulsion. The upper ball is now shifted horizontally by a distance  $d$  ( $d \ll h$ ) to the right and then both the balls are released. Which way will the balls move immediately after this?
- A. ball on the surface moves towards left, ball above moves downwards.
  - B. both balls remain static at their new positions.
  - C. ball on the surface moves towards right and ball above moves upwards.
  - D. both balls oscillate around their original positions.
10. Consider the standard notation of discrete finite groups with  $\mathbb{Z}_n$  corresponding to the rotation by  $2\pi/n$  about a given axis,  $S_n$  corresponding to the permutation group of the set  $S$  having  $n$  elements, i.e.  $S = \{1, 2, 3, \dots, n\}$ , and the Dihedral group  $D_n$  corresponding to the reflection and rotation symmetries of a regular polygon with  $n$  number of sides. Which of the following is the smallest non-abelian group?
- A.  $S_3$
  - B.  $\mathbb{Z}_3$
  - C.  $D_4$
  - D.  $S_4$

## Part B: 3-mark MCQ

1. Consider a  $2 \times 2$  matrix  $A = \begin{bmatrix} 0 & 1 \\ 1 & 1 \end{bmatrix}$  which has eigenvalues  $\lambda_1 = \frac{1+\sqrt{5}}{2}$  and  $\lambda_2 = \frac{1-\sqrt{5}}{2}$ . For any natural number  $n$  which of the following is correct ?

A.  $A^n = \frac{1}{\sqrt{5}} \begin{bmatrix} \lambda_1^{n-1} - \lambda_2^{n-1} & \lambda_1^n - \lambda_2^n \\ \lambda_1^n - \lambda_2^n & \lambda_1^{n+1} - \lambda_2^{n+1} \end{bmatrix}$

B.  $A^n = \frac{1}{\sqrt{5}} \begin{bmatrix} \lambda_1^{n-1} - \lambda_2^{n-1} & \lambda_1^n + \lambda_2^n \\ \lambda_1^n + \lambda_2^n & \lambda_1^{n+1} - \lambda_2^{n+1} \end{bmatrix}$

C.  $A^n = \frac{1}{\sqrt{5}} \begin{bmatrix} \lambda_1^{n-1} + \lambda_2^{n-1} & \lambda_1^n - \lambda_2^n \\ \lambda_1^n - \lambda_2^n & \lambda_1^{n+1} + \lambda_2^{n+1} \end{bmatrix}$

D.  $A^n = \frac{1}{\sqrt{5}} \begin{bmatrix} \lambda_1^{n-1} + \lambda_2^{n-1} & \lambda_1^n + \lambda_2^n \\ \lambda_1^n + \lambda_2^n & \lambda_1^{n+1} + \lambda_2^{n+1} \end{bmatrix}$

2. A quantum mechanical system is spanned by the eigenstates  $|a_1\rangle$  and  $|a_2\rangle$  of a Hermitian operator  $A$  with eigenvalues  $a_1$  and  $a_2$  respectively. If there is no degeneracy, what is the expectation value of the operator  $(A - a_1)(A - a_2)$  in the state  $\frac{|a_1\rangle + |a_2\rangle}{\sqrt{2}}$ ?

A. 0

B. 1

C.  $(a_2 - a_1)(a_1 - a_2)$

D.  $\frac{(a_2 - a_1)(a_1 - a_2)}{2}$

3. Three observers successively measure the spin of a given proton along z-axis, x-axis and again z-axis, respectively. The first observer finds the spin projection to be  $+\frac{1}{2}$ . Assuming no other factors, what is the probability that the third observer finds the spin projection to be  $-\frac{1}{2}$ ?

A. 0.5

B. 1

C. 0

D. None of the others

4. A capacitor with capacitance  $C$  is connected in series with a resistor of resistance  $R$  and an ideal DC source with voltage  $V_S$ . At one instant during the charging of the capacitor if the resistor is replaced by a wire of zero resistance, which of the following statements is true?
- The capacitor immediately attains the source voltage  $V_S$ .
  - The voltage across the capacitor will drop immediately to zero.
  - The voltage across the capacitor will increase slowly.
  - None of the others is true.
5. Calculate the partition function for two indistinguishable bosonic particles at a temperature  $T$ , which can be distributed in two single-particle energy levels  $\epsilon_1$  and  $\epsilon_2$ . Consider  $\beta = \frac{1}{k_B T}$ .
- $e^{-2\beta\epsilon_1} + e^{-2\beta\epsilon_2} + e^{-\beta(\epsilon_1+\epsilon_2)}$
  - $\frac{1}{2!} (e^{-\beta\epsilon_1} + e^{-\beta\epsilon_2})^2$
  - $(e^{-\beta\epsilon_1} + e^{-\beta\epsilon_2})^2$
  - $e^{-2\beta\epsilon_1} + e^{-2\beta\epsilon_2} + e^{-2\beta(\epsilon_1+\epsilon_2)}$
6. For a particle in a one-dimensional box of width  $L$ , the uncertainty  $\Delta p$  in momentum in the  $n$ -th eigenstate of energy for large  $n$  is
- $\frac{n\pi\hbar}{L}$
  - $\frac{2n\pi\hbar}{L}$
  - $\frac{2n\hbar}{L}$
  - $\frac{\hbar}{n\pi L}$
7. Consider a circular disk of radius  $R$  and mass  $M$  in the X-Y plane, with a surface mass density  $\sigma(r) = \sigma_0 e^{-r^2/a}$ , where  $r$  is the distance from the center of the disk. What is the moment of inertia around the Z-axis through the center of the disk? [consider  $R \gg a$ ]
- $Ma^2$
  - $\frac{1}{3}Ma^2$
  - $6Ma^2$
  - $\frac{1}{2}Ma^2$

8. For a one-dimensional simple harmonic oscillator with mass  $m$  and angular frequency  $\omega$ , consider a perturbation  $\lambda x^4$  in the Hamiltonian ( $\lambda > 0$ ). What is the lowest order correction to the ground state energy?

[The position operator expressed in terms of the raising and lowering operators is  $\hat{x} = \sqrt{\frac{\hbar}{2m\omega}} (\hat{a} + \hat{a}^\dagger)$ .]

- A.  $\frac{3\lambda}{4} \left(\frac{\hbar}{m\omega}\right)^2$
- B.  $\frac{3\lambda}{2} \left(\frac{\hbar}{m\omega}\right)^2$
- C.  $\frac{5\lambda}{2} \left(\frac{\hbar}{m\omega}\right)^2$
- D.  $\frac{5\lambda}{4} \left(\frac{\hbar}{m\omega}\right)^2$

9. The time averaged electrostatic potential of a neutral H-atom is given by

$$\Phi(\vec{r}) = \frac{q}{4\pi\epsilon_0} \frac{e^{-\alpha r}}{r} \left(1 + \frac{\alpha r}{2}\right)$$

The classical charge distribution corresponding to this is

- A.  $-\frac{q}{8\pi}\alpha^3 e^{-\alpha r} + q\delta^3(\vec{r})$
- B.  $qe^{-\alpha r} \left(1 + \frac{\alpha r}{2}\right)$
- C.  $-\frac{q}{8\pi}\alpha^3 e^{-\alpha r}$
- D.  $\frac{q}{8\pi}\alpha^3 e^{-\alpha r} \left(1 + \frac{\alpha r}{2}\right) - q\delta^3(\vec{r})$

10. Given an isolated thermodynamic system with a total energy  $E$ , total volume  $V$  and total number of particles  $N$ , the condition for stable thermal equilibrium, in terms of its entropy  $S$  under small changes  $\Delta E$  and  $\Delta V$ , is given by

- A.  $S(E + \Delta E, V + \Delta V, N) + S(E - \Delta E, V - \Delta V, N) - 2S(E, V, N) < 0$
- B.  $S(E + \Delta E, V + \Delta V, N) + S(E - \Delta E, V - \Delta V, N) + 2S(E, V, N) < 0$
- C.  $-S(E + \Delta E, V + \Delta V, N) + S(E - \Delta E, V - \Delta V, N) - 2S(E, V, N) < 0$
- D.  $S(E + \Delta E, V + \Delta V, N) - S(E - \Delta E, V - \Delta V, N) - 2S(E, V, N) < 0$

11. Consider the group  $S_4$  corresponding to the permutations of the set  $S$  having four elements, say  $S = \{1, 2, 3, 4\}$ . How many non-identity self-inverse (i.e. order 2) elements does  $S_4$  have?
- A. 9
  - B. 6
  - C. 8
  - D. 12
12. The volume of a nucleus, treated as a Fermi gas in three-dimensional space, is proportional to the number of fermions present in it. If the total number of fermions is changed from  $N$  to  $\frac{1}{2}N$ , the total energy of the system will
- A. be doubled.
  - B. remain the same.
  - C. be 4 times its original value.
  - D. be half of its original value.
13. Consider a two-dimensional Fermi gas at 0 K with Fermi energy  $\epsilon_F$ . The average energy per particle of this gas is:
- A.  $\frac{\epsilon_F}{2}$
  - B.  $\frac{3\epsilon_F}{5}$
  - C.  $\frac{\epsilon_F}{3}$
  - D.  $\frac{\epsilon_F}{4}$

14. A block, suspended from a massless spring, is fully immersed in a liquid contained in a reservoir. What is the time period of small oscillations of the block?

[Given: Mass of the block  $m$ , density of the block  $\rho_b$ , natural length of the spring  $L$ , spring constant  $k$ , acceleration due to gravity  $g$ , density of the liquid  $\rho_l$ , damping coefficient of the liquid i.e., damping per unit mass per unit velocity  $\gamma$ .]

A.  $2\pi\sqrt{\frac{1}{k/m - \gamma^2/4}}$

B.  $2\pi\sqrt{\frac{1}{k/m + \gamma^2/4}}$

C.  $2\pi\sqrt{\frac{L}{(1 - \rho_l/\rho_b)g}}$

D.  $2\pi\sqrt{\frac{m}{k}}$

15. A circular loop of radius  $a$ , carrying a current  $I$  in an anticlockwise direction (when seen downwards from the positive  $Z$  axis), is placed on the  $X$ - $Y$  plane centered at the origin. What is the magnetic field on the  $X$ - $Y$  plane at  $r \gg a$ ?

A.  $\frac{\mu_0 I}{4} \frac{a^2}{r^3}$  in the negative  $Z$  direction

B.  $\frac{\mu_0 I}{4\pi} \frac{a^2}{r^3}$  in the positive  $Z$  direction

C. 0

D.  $\frac{\mu_0 I}{4} \frac{a^2}{r^3} \hat{r}$

16. Evaluate  $\vec{\nabla} \cdot (r^4 \vec{r})$ , where  $\vec{r}$  represents a three dimensional position vector.

A.  $7r^4$

B.  $5r^4$

C.  $r^4$

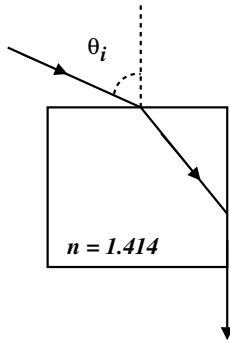
D. 0



17. A particle is moving with velocity  $v_x = v_y = v_z = c/2$  in frame  $S$ . The ratio of velocity component  $v_y$  to the velocity component  $v_{y'}$  as measured in frame  $S'$  moving with velocity  $c/2$  with respect to frame  $S$  along the common  $x$  direction is

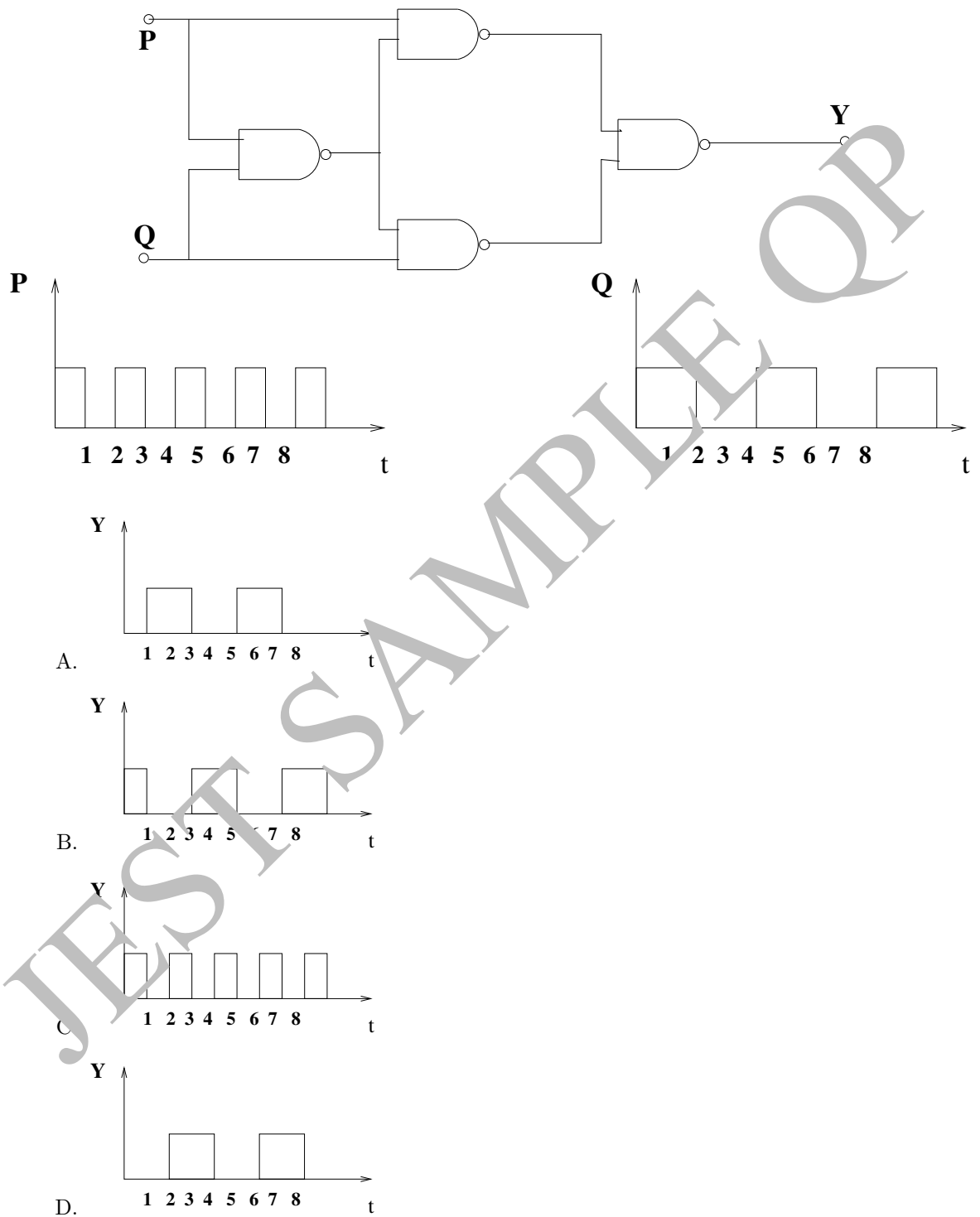
- A.  $\cos(\pi/6)$
- B.  $\cos(\pi/3)$
- C.  $\sin(\pi/6)$
- D.  $\sin(\pi/3)$

18. A ray of light is incident on a glass cube of refractive index 1.414 as shown in the figure. Find the angle of incidence  $\theta_i$ , such that the ray grazes down the side of the glass cube.



- A.  $\pi/2$
- B.  $\pi/3$
- C.  $\pi/4$
- D. 0

19. For the circuit and the inputs P and Q shown, which of the following is the correct output Y?



20. A silicon p-n junction diode operates at 27°C. The current  $I$  is doubled when the forward bias is increased. The increase in the forward bias is closest to:

[Assume  $I \gg I_s$ , where  $I_s$  is the reverse saturation current and the emission coefficient  $\eta_{Si} = 2$ .]

- A. 36 mV
- B. 18 mV
- C. 72 mV
- D. 54 mV

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## Part C: 3-Mark Numerical

- Given the mass of the proton  $m_p \simeq 1836 m_e$  and mass of the deuteron  $m_d \simeq 3670 m_e$ , where  $m_e$  is the electron mass, find the fractional shift (in parts per million, to the nearest integer) of the ground state energy of the deuterium atom as compared to H-atom.
- If a resistor of  $10 k\Omega$  and a capacitor of  $0.5 \mu\text{F}$  are connected in series across an AC supply of 220 V (rms) at 50 Hz, what is the average power (in mW, to the nearest integer) dissipated in the circuit?
- The average lifetime of a muon in its rest frame is 2200 ns. What will be the average distance (in meters, to the nearest integer) travelled by it, when created with a velocity of  $\frac{1}{5}c$ , before it decays? Here  $c$  is the speed of light.
- What is the value of the integral

$$I = \frac{3}{2\pi} \oint_{\mathcal{C}} \frac{dz}{1+z^2}$$

where the contour  $\mathcal{C}$  is a circle of radius 2 centered at the origin?

- A simple pendulum with effective length  $l$  and a bob of mass  $m$  has a time period  $T_1$ . Suppose now that the bob is given an electric charge  $+Q$ . It is made to oscillate just above a two dimensional infinite sheet with surface charge density  $+\sigma$ , where  $\frac{Q\sigma}{mg} = \frac{3}{2}$ ,  $\epsilon_0$  being the permittivity of free space and  $g$  being the acceleration due to gravity. If the period of oscillation in this case is  $T_2$ , determine  $\frac{T_2}{T_1}$ . [Neglect radiation from the charge.]
- The Fraunhofer diffraction intensity pattern for light of wavelength  $\lambda$  by a single slit of width  $a$  is given by

$$I = A_0^2 \left( \frac{\sin \beta}{\beta} \right)^2$$

where  $A_0$  is the intensity of the central maximum and  $\beta = \frac{\pi a \sin \theta}{\lambda}$ , where  $\theta$  is the angle with the incident beam. What is the angular separation in milli-radians, between the two first minima on two sides of the central beam, if  $a = 1 \text{ mm}$  and  $\lambda = 5000 \text{ \AA}$ ?

- A heat engine works between a high temperature source and a sink at  $27^\circ\text{C}$ . If the maximum efficiency possible for it to achieve is 50%, what is the temperature of the source in  $^\circ\text{C}$ ?
- Suppose the wave function of a free particle in one dimension obeys  $\frac{d^2\psi}{dx^2} = -4\psi$  in units where  $\hbar = 1$ . What is the magnitude of the momentum of the particle?

9. A current of  $10A$  is maintained for  $1s$  in a resistor of resistance  $25\ \Omega$ , which is thermally insulated. The initial temperature of the resistor is  $23^{\circ}C$ . The resistor has a mass of  $10\text{ gm}$  and a specific heat of  $836\text{ Jkg}^{-1}\text{K}^{-1}$ . What is the entropy change of the resistor, rounding off to the nearest whole number in units of  $\text{JK}^{-1}$  ?
10. A  $3 \times 3$  matrix  $M$  satisfies  $M^2 - 3M + 2I = 0$ . Find the determinant of the matrix  $M$  if its trace is 6.

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